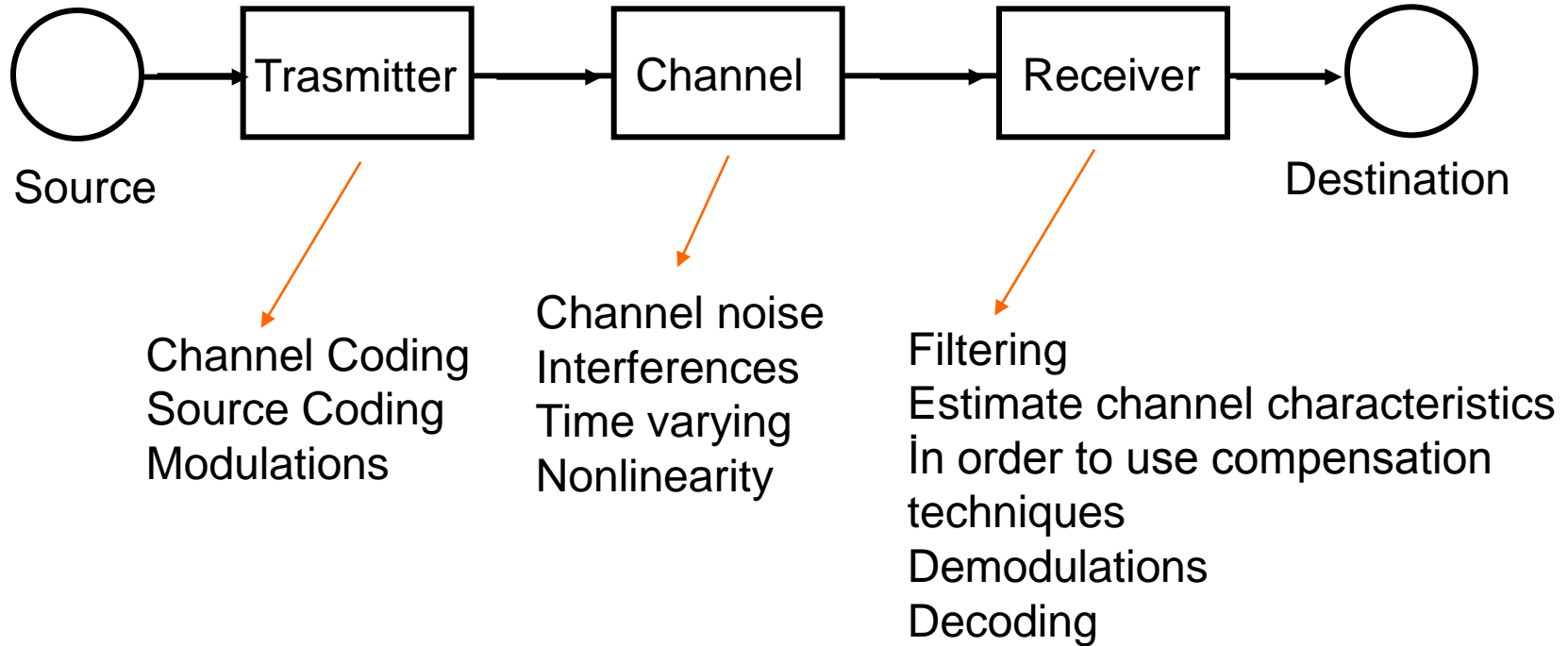


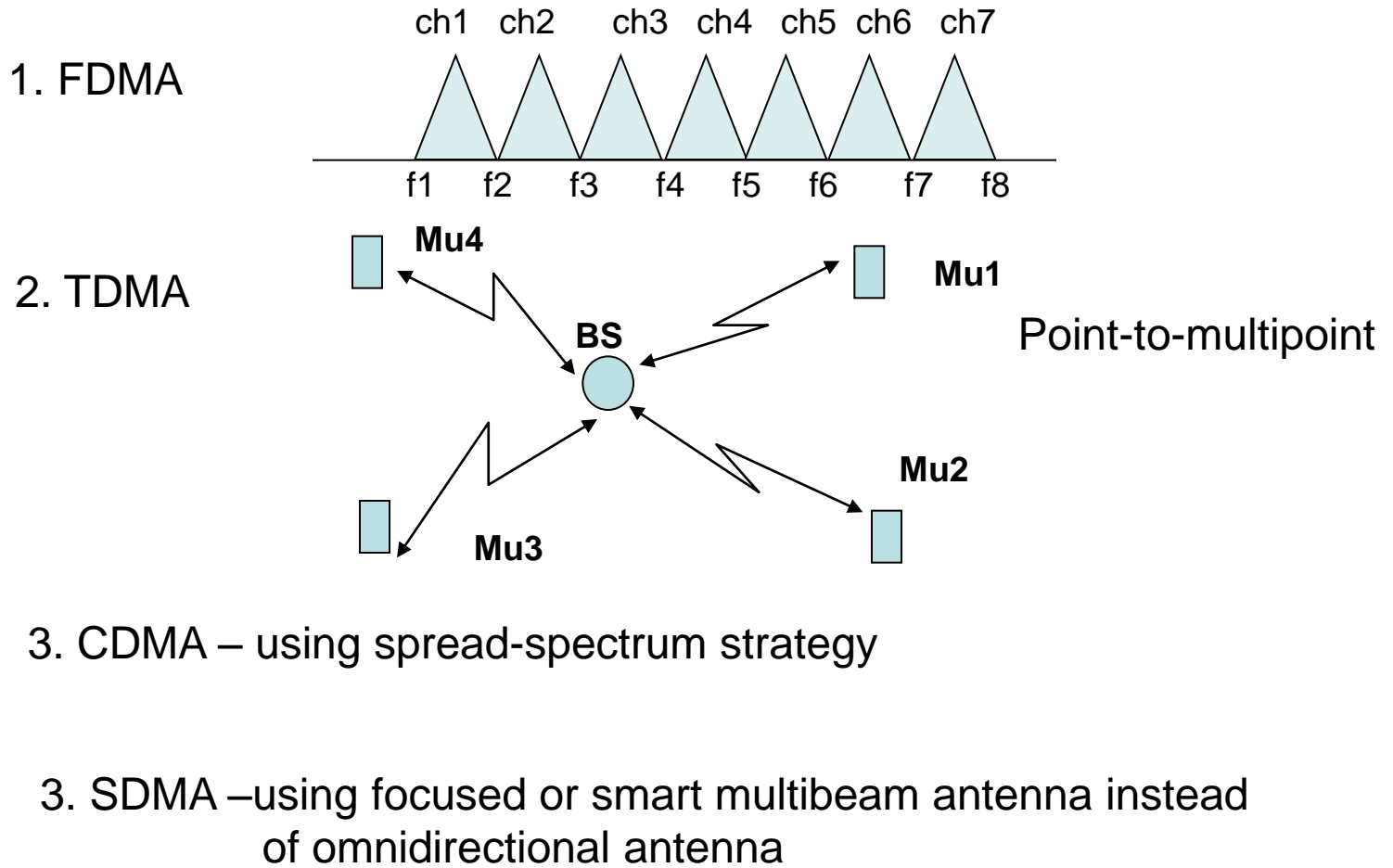
# Fundamentals of Radio communications

## 1. Physical Layer

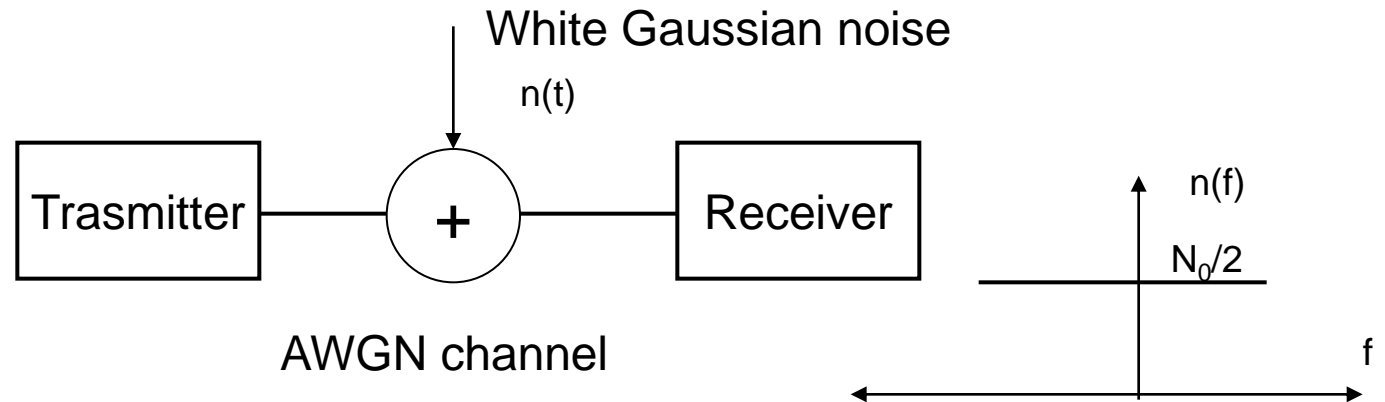


## 2. Data-Link Layer

General approach to sharing the physical resources among the different users.



# Channel Models

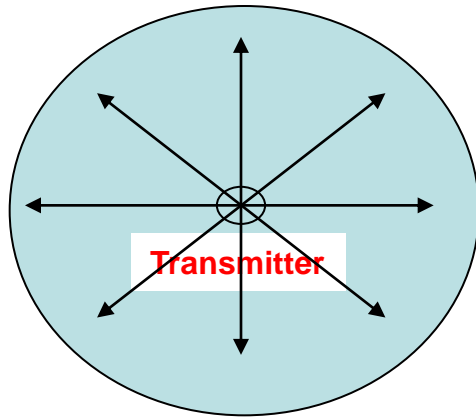


AWGN : zero mean, having Gaussian distribution and two sided power spectral density

1. Physical model-take into account the exact physics of propogation environment
  1. Free-space (line-of-site) propogation
  2. Reflection-bouncing of EW from surrounding objects(buidings, montains,..)
  3. Diffraction-bending of EW around objects
2. Statistical model (emprical approach)-measuring propogation characteristic in a variety of environment and developping probobalistic model

# Free-Space Propagation

Power Density at distance R of isotropic antenna  
(that transmits equally in all directions)



$$P_D = \frac{P_T G_T}{4\pi R^2}$$

○  
Receiver

Received Power:

$$P_R = A_{\text{eff}} P_D = \frac{A_{\text{eff}} P_T G_T}{4\pi R^2}$$

## Receiving Antenna Effective Area:

$$\mathbf{A}_{\text{eff}} = \frac{\lambda^2 \mathbf{G}_R}{4\pi}$$

$$\mathbf{P}_R = \frac{\mathbf{P}_T \mathbf{G}_T \mathbf{G}_R}{(4\pi \mathbf{R} / \lambda)^2} = \frac{\mathbf{P}_T \mathbf{G}_T \mathbf{G}_R}{L}; L = \left(\frac{4\pi \mathbf{R}}{\lambda}\right)^2$$

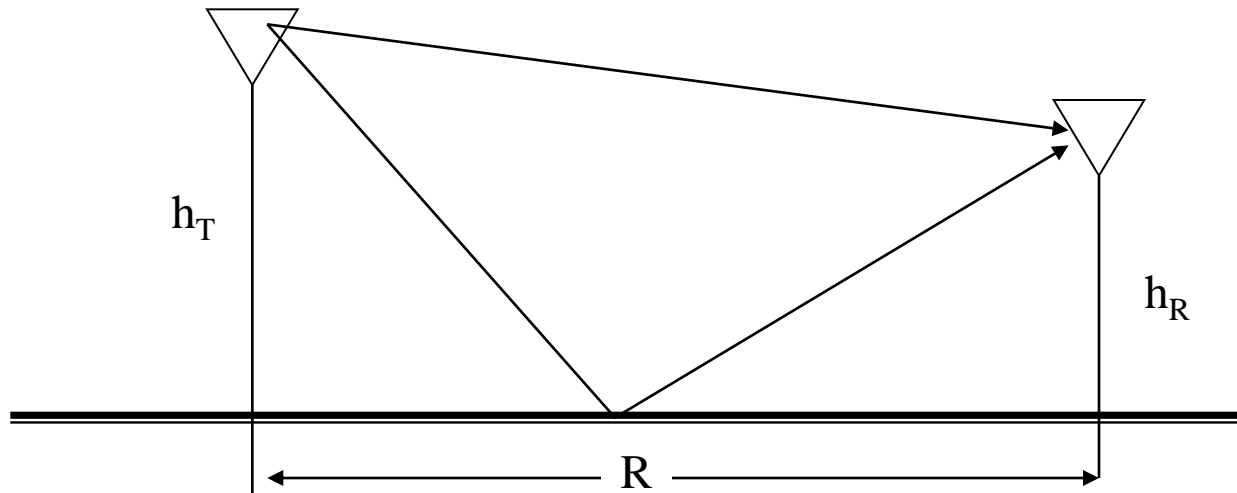
$$\mathbf{R} = \frac{\lambda}{4\pi} \sqrt{L} = \frac{c}{4\pi} \mathbf{f} \sqrt{L}$$

**L - free-space path loss**

**Friis's Formula expresses the attenuation of free space**

$$\mathbf{P}_R \text{ (dB)} = \mathbf{P}_T \text{ (dB)} + \mathbf{G}_T \text{ (dB)} + \mathbf{G}_R \text{ (dB)} - \mathbf{L} \text{ (dB)}$$

# Plane Earth Propagation Model



$$P_R = 4P_T \left( \frac{\lambda}{4\pi R} \right)^2 G_T G_R \text{Sin}^2 \left( \frac{2\pi h_T h_R}{\lambda R} \right)$$

If  $\lambda R \gg h_T h_R$

$$P_R = P_T G_T G_R \left( \frac{h_T h_R}{R^2} \right)^2$$

$$P_R = \frac{P_T G_T G_R}{(4\pi R / \lambda)^2} = \frac{P_T G_T G_R}{(4\pi R)^2} \lambda^2$$

# Antenna Gain

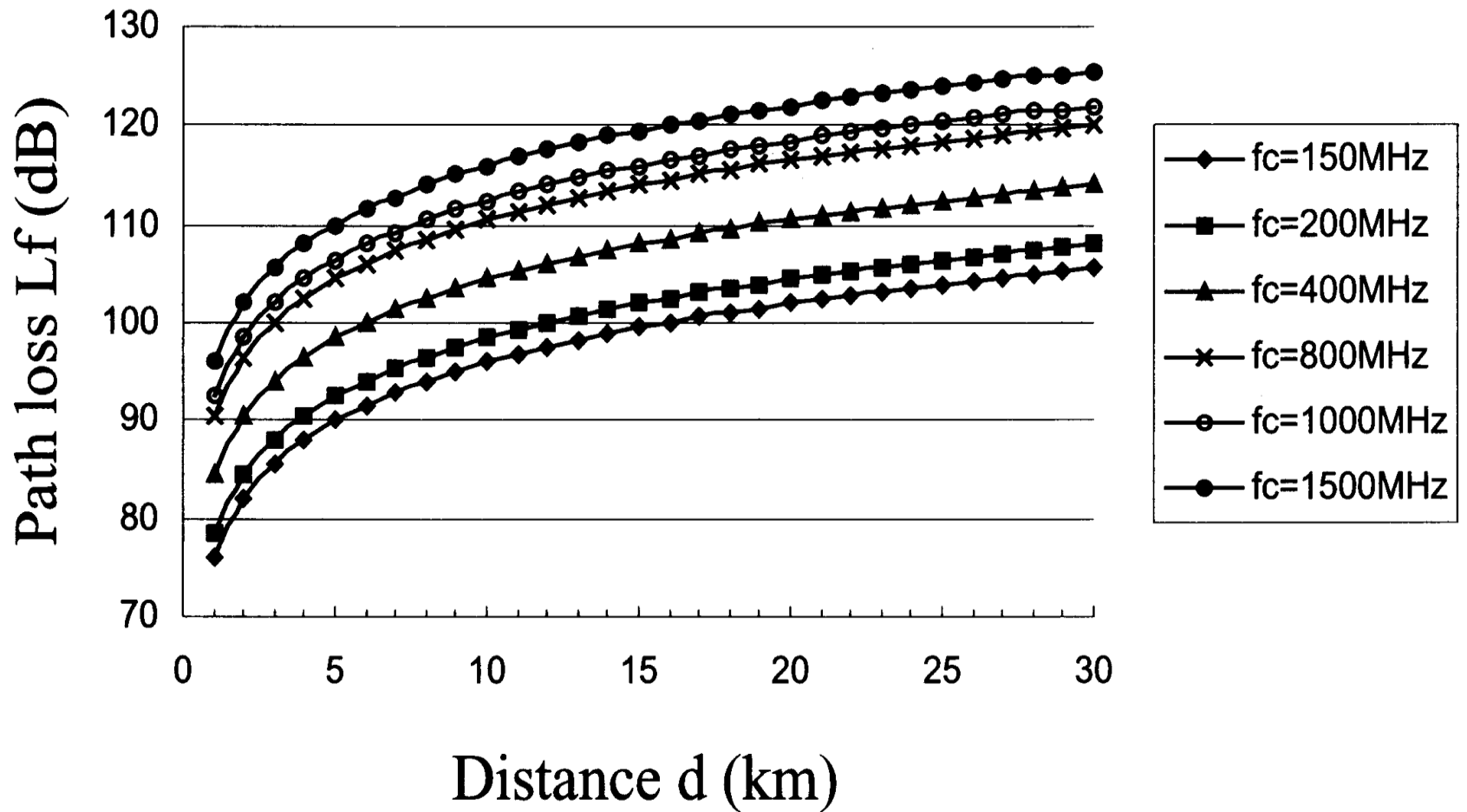
$$\mathbf{G} = \frac{4\pi}{\lambda^2} \mathbf{A}_e$$

**For Parabolic Antenna**

$$\mathbf{A}_e = \eta \frac{\pi \mathbf{D}^2}{4}$$

$$\mathbf{G} = \frac{\mathbf{A}_e}{\mathbf{A}_i} = \frac{\eta \pi \mathbf{D}^2 / 4}{\lambda^2 / 4\pi} = \eta \left( \frac{\pi \mathbf{D}}{\lambda} \right)^2$$

**Antenna efficiency  $\eta = 0.5-0.7$**





# Terrestrial Propagation: Statistical Model

1. Median Path Loss
2. Local Variations

$$\frac{P_R}{P_T} = \frac{\beta}{r^n}$$

n-path-loss exponent , n=2-5;

$$\beta = F(f, h_R, h_T)$$

Right-side hand can be written

$$L_p = \beta_0(\text{dB}) - 10 \log_{10}(r/r_0)$$

Environment	n
Free-space	2
Flat rural	3
Rolling rural	3.5
Suburban, low rise	4
Dense urban	4.5

$\beta_0(\text{dB})$  – free-space path loss at reference distance  $r_0$

# Local Propagation Loss. Log-Normal Shadowing

Log normal distribution describe the random shadowing effect thjat is releted variation of median path loss with local characteristics

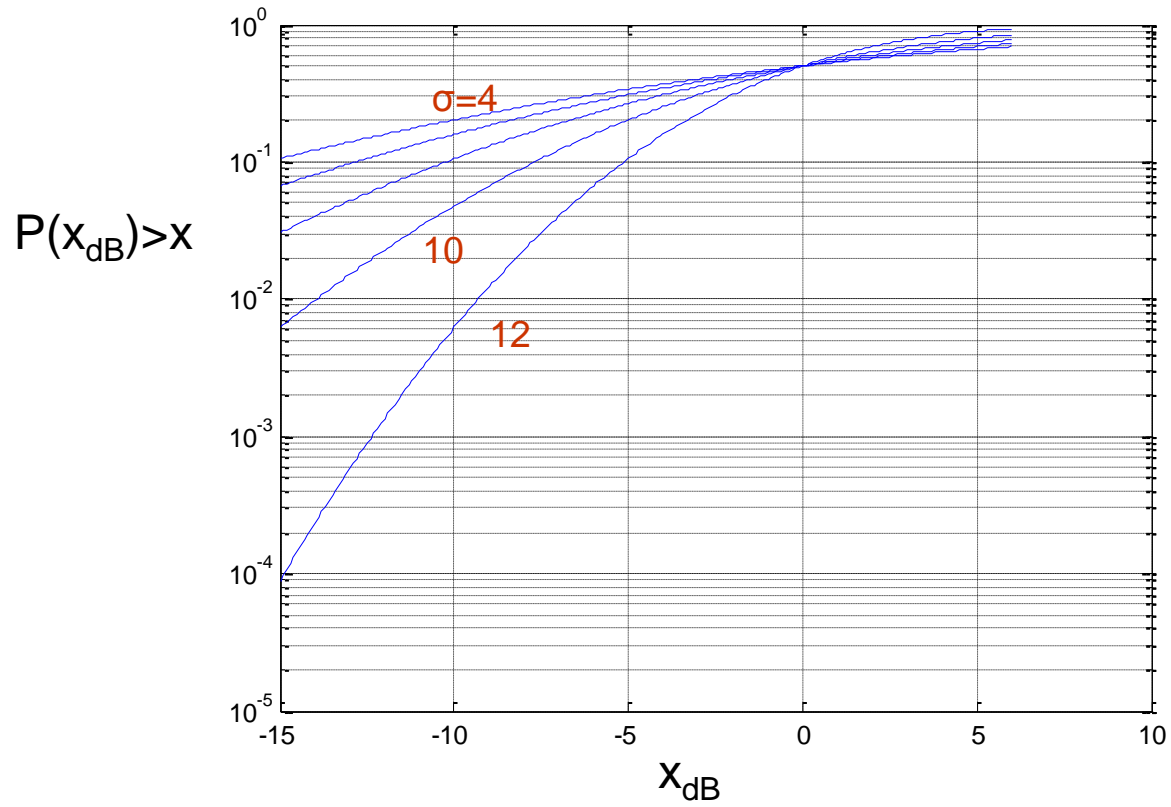
$$L_p = \beta_0(\text{dB}) - 10\log_{10}(r/r_0) + X\sigma$$

$X\sigma$ -zero mean gaussian random variable with standart deviation  $\sigma$

$$f(x_{dB}) = \frac{1}{\sigma_{dB}\sqrt{2\pi}} e^{-\frac{(x_{dB}-\mu_{50})^2}{2\sigma_{dB}^2}}$$

$\sigma_{dB} = 5-12$  dB;  $\mu_{50}$ -median value path loss;  $x_{dB}$ - random variable

$$P(x_{dB} > x) = \int_x^{\infty} f(x_{dB}) dx_{dB}$$



To find the probability that the received signal level will exceed a particular level Q-function is used

$$Q(z) = \frac{1}{\sqrt{2\pi}} \int_z^{\infty} e^{-\frac{x^2}{2}} dx = \frac{1}{2} [1 - \operatorname{erf}(\frac{z}{\sqrt{2}})];$$

where  $Q(z) = 1 - Q(-z)$

The probability that the received signal level will exceed a particular level  $\gamma$  can be calculated

$$P_R(P_R(R) > \gamma) = Q\left(\frac{\gamma - Lp}{\sigma}\right)$$

$$P_R(P_R(R) < \gamma) = Q\left(\frac{Lp - \gamma}{\sigma}\right)$$

The fraction of the coverage area in which the received signal exceeds receiver sensitivity  $S_m$  can be calculated

$$\mathbf{Fu} = \frac{\mathbf{1}}{\mathbf{2}} \left\{ \mathbf{1} - \mathbf{erf}(\mathbf{a}) + \mathbf{e}^{\frac{\mathbf{1}-\mathbf{2ab}}{\mathbf{b}^2}} \left[ \mathbf{1} - \mathbf{erf}\left(\frac{\mathbf{1}-\mathbf{ab}}{\mathbf{b}}\right) \right] \right\}$$

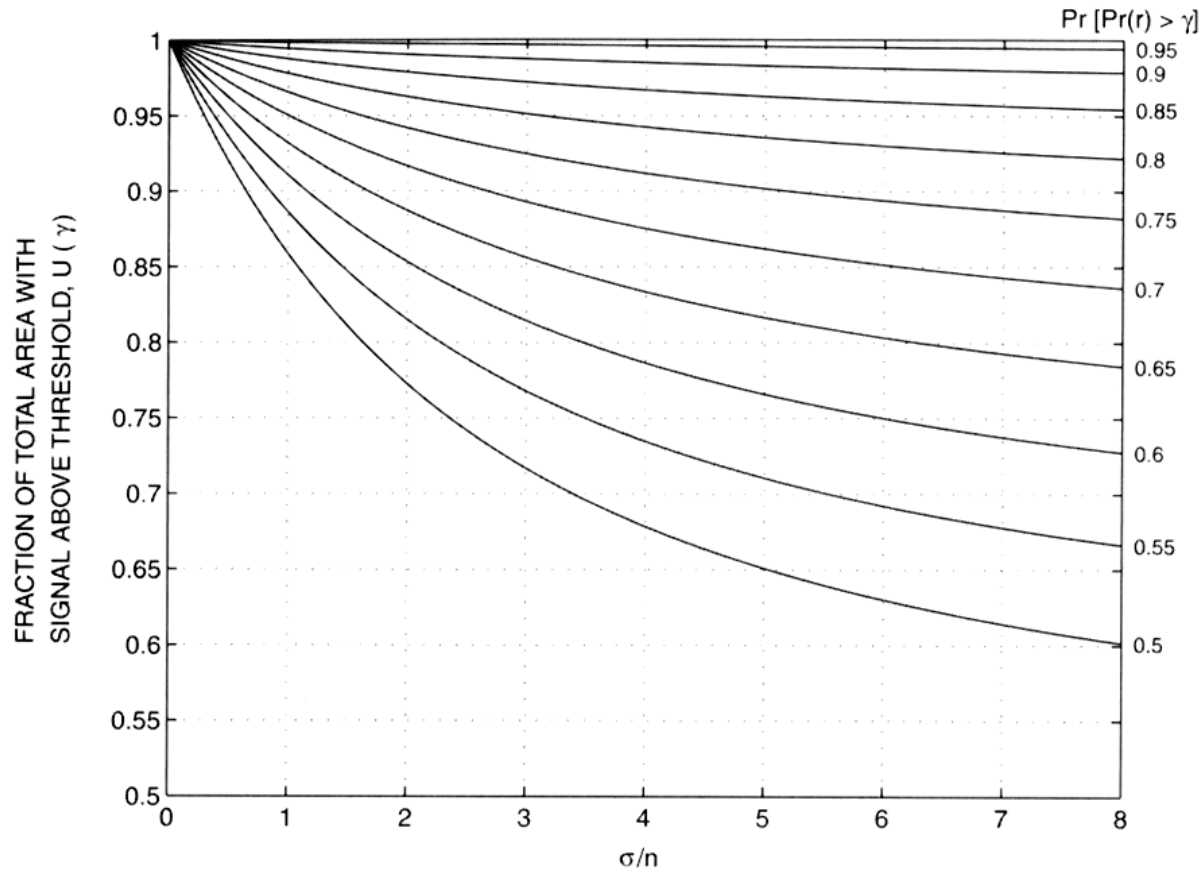
$$\mathbf{a} = (\mathbf{S}_m - \mathbf{P}_T + \beta_0 + 10 \log_{10}(r/r_0)) / \sigma \sqrt{2}$$

$$\mathbf{b} = 10 n \log(r/r_0) / \sigma \sqrt{2}$$

If  $m_0 = S_m$ , at  $r = r_0$  then  $a = 0$

$$\mathbf{Fu} = \frac{\mathbf{1}}{\mathbf{2}} \left\{ \mathbf{1} + \mathbf{e}^{\frac{\mathbf{1}}{\mathbf{b}^2}} \left[ \mathbf{1} - \mathbf{erf}\left(\frac{\mathbf{1}}{\mathbf{b}}\right) \right] \right\}$$

# Area versus Distance coverage model with shadowing model



**Figure 4.18** Family of curves relating fraction of total area with signal above threshold,  $U(\gamma)$  as a function of probability of signal above threshold on the cell boundary.