Chapter 6: Mechanical Properties

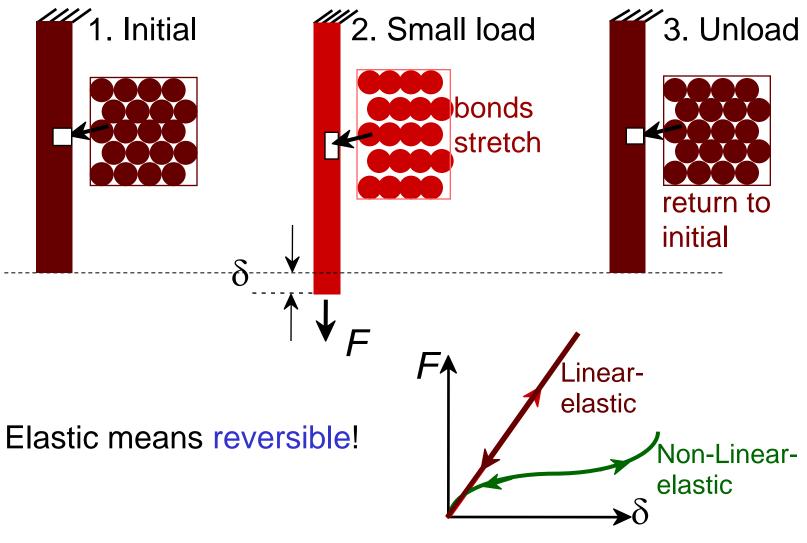
ISSUES TO ADDRESS...

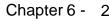
- Stress and strain: What are they and why are they used instead of load and deformation?
- Elastic behavior: When loads are small, how much deformation occurs? What materials deform least?
- Plastic behavior: At what point does permanent deformation occur? What materials are most resistant to permanent deformation?
- Toughness and ductility: What are they and how do we measure them?



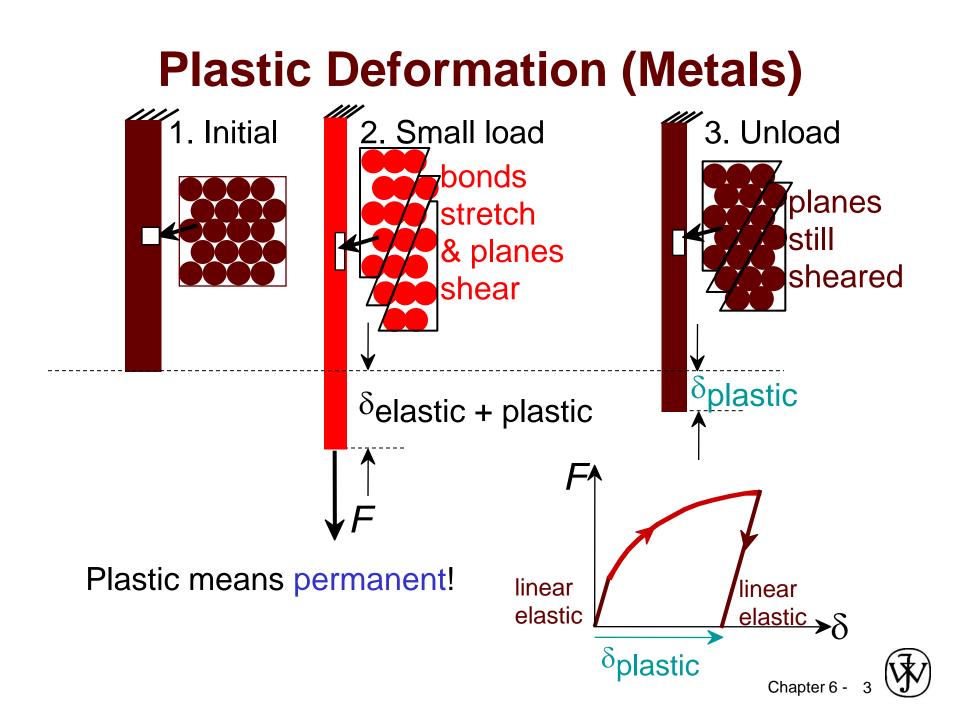
Chapter 6

Elastic Deformation

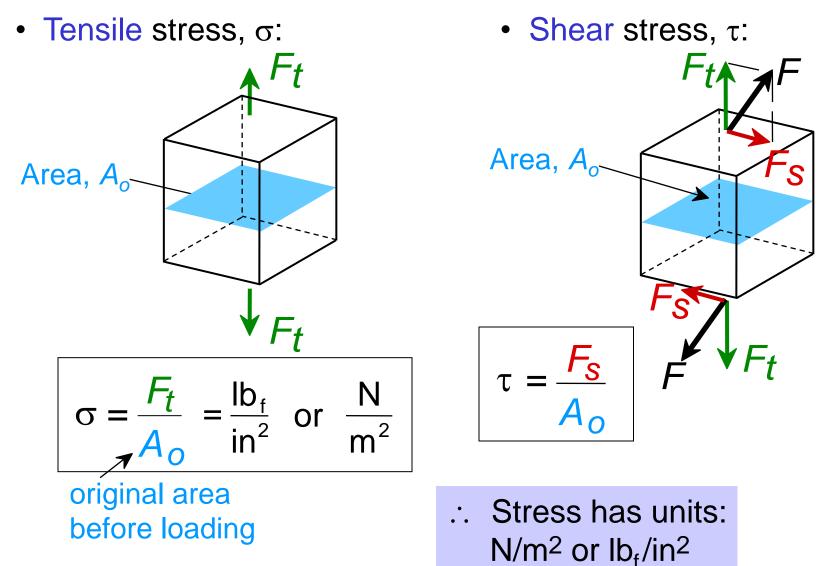








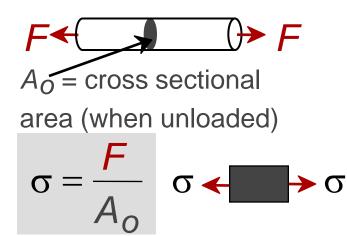
Engineering Stress





Common States of Stress

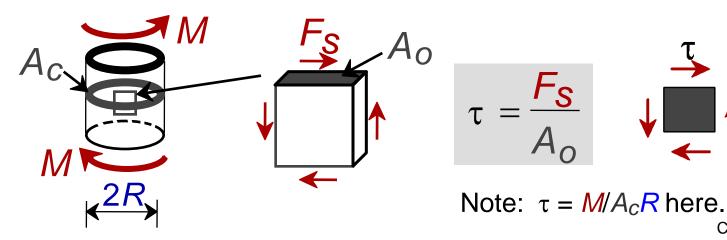
• Simple tension: cable-





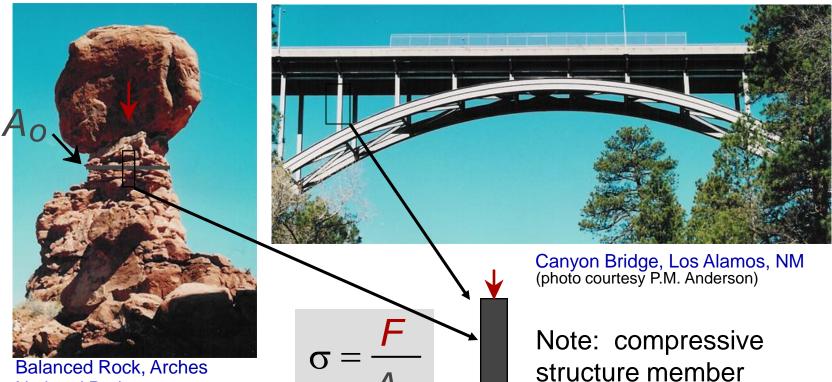
• Torsion (a form of shear): drive shaft

Ski lift (photo courtesy P.M. Anderson)



OTHER COMMON STRESS STATES (i)

• Simple compression:



National Park (photo courtesy P.M. Anderson) $(\sigma < 0 here).$

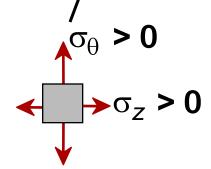


OTHER COMMON STRESS STATES (ii)

• **Bi-axial** tension:

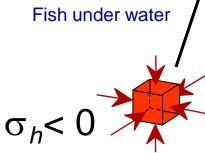


Pressurized tank (photo courtesy P.M. Anderson)



• Hydrostatic compression:



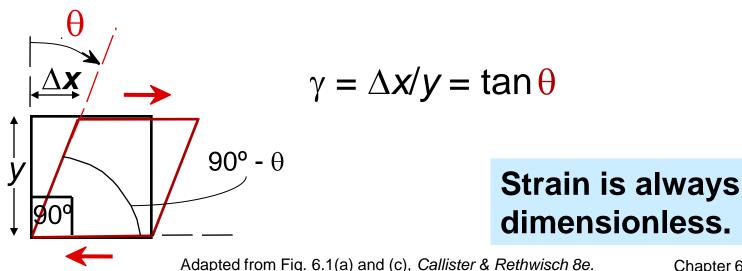


(photo courtesy P.M. Anderson)



Engineering Strain

- Tensile strain: Lateral strain: δ/2 $\varepsilon = \frac{\delta}{L_o}$ <u>1</u>3 L_{o} Wo W_{0}
- Shear strain:



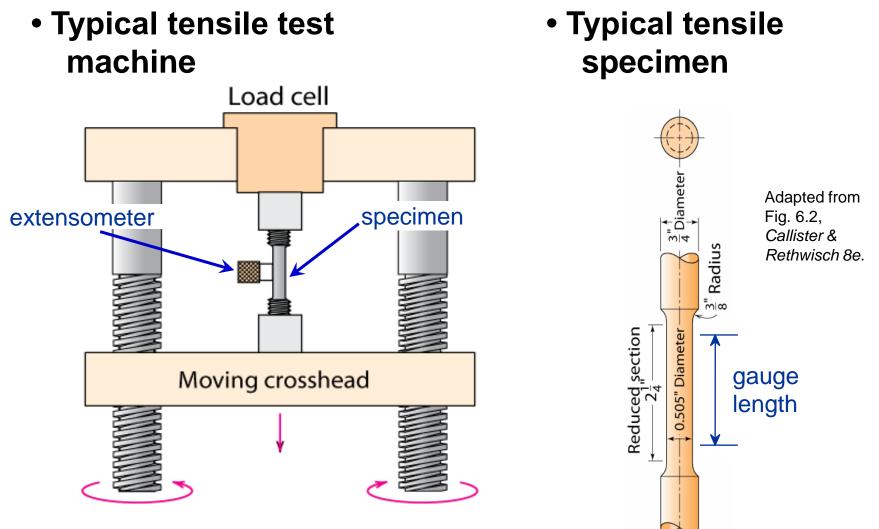


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Chapter 6 -

Adapted from Fig. 6.1(a) and (c), Callister & Rethwisch 8e.

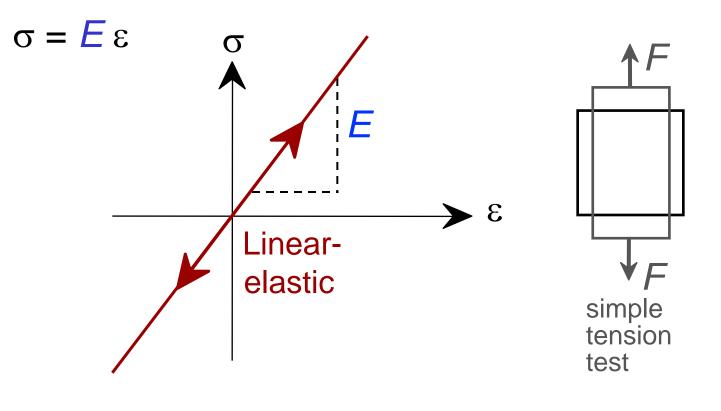
Stress-Strain Testing



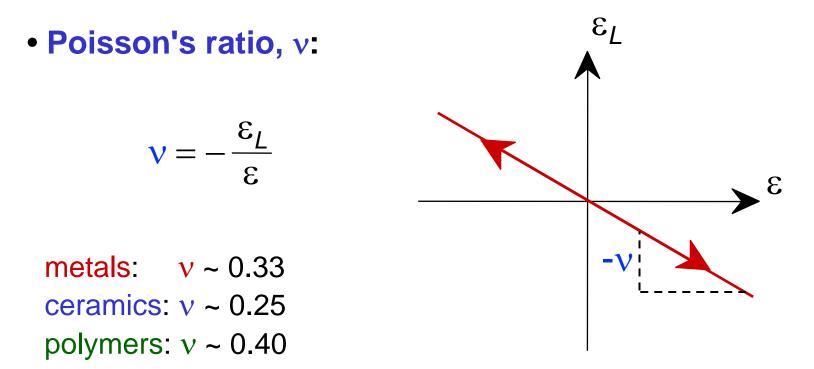
Adapted from Fig. 6.3, *Callister & Rethwisch 8e.* (Fig. 6.3 is taken from H.W. Hayden, W.G. Moffatt, and J. Wulff, *The Structure and Properties of Materials*, Vol. III, *Mechanical Behavior*, p. 2, John Wiley and Sons, New York, 1965.)

Linear Elastic Properties

- Modulus of Elasticity, E: (also known as Young's modulus)
- Hooke's Law:



Poisson's ratio, v



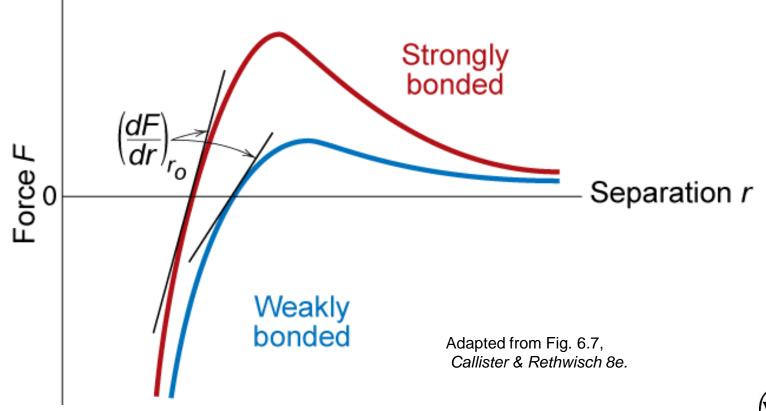
Units: *E*: [GPa] or [psi] v: dimensionless

- v > 0.50 density increases
- v < 0.50 density decreases (voids form)



Mechanical Properties

 Slope of stress strain plot (which is proportional to the elastic modulus) depends on bond strength of metal

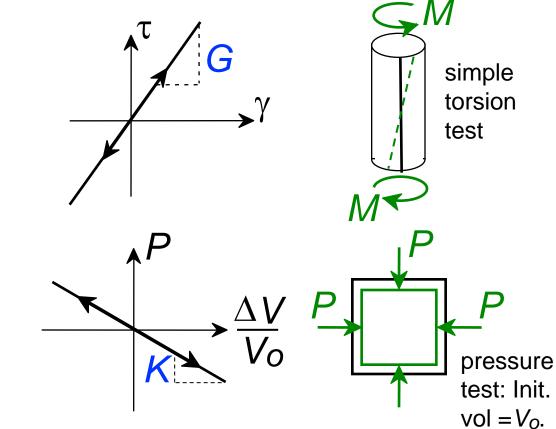


Other Elastic Properties

• Elastic Shear modulus, G:

 $\tau = \mathbf{G} \gamma$

• Elastic Bulk modulus, K: $P = -K \frac{\Delta V}{V_{O}}$



• Special relations for isotropic materials:

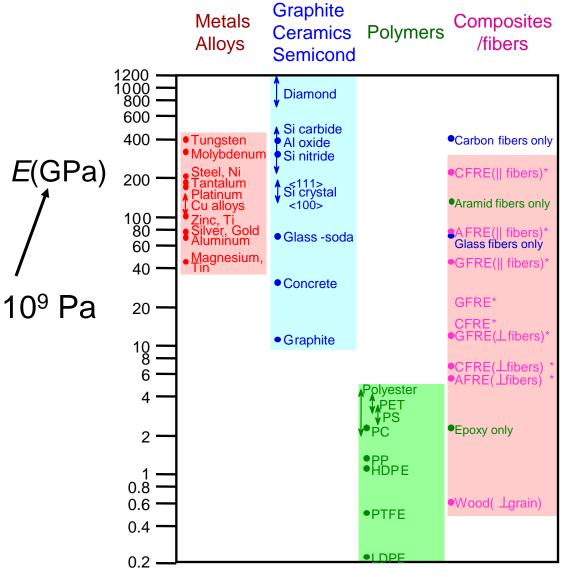
$$G = rac{E}{2(1+v)}$$
 $K = rac{E}{3(1-2v)}$



Vol chg.

 $= \Delta V$

Young's Moduli: Comparison

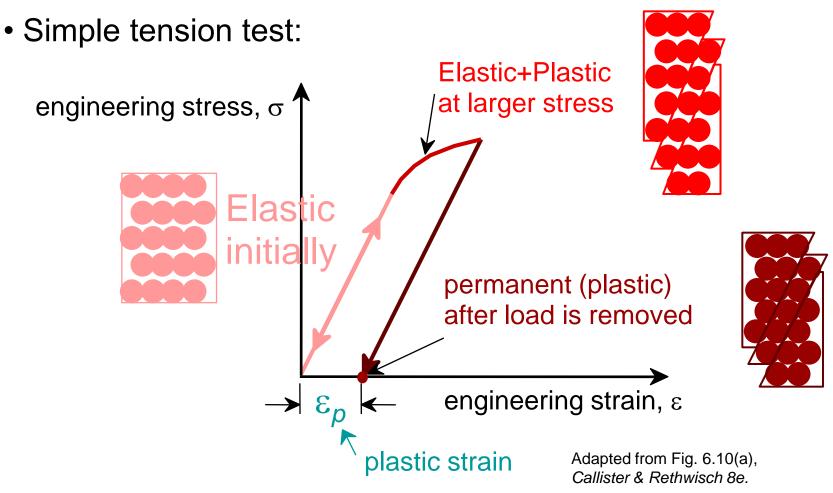


Based on data in Table B.2, *Callister & Rethwisch 8e.* Composite data based on reinforced epoxy with 60 vol% of aligned carbon (CFRE), aramid (AFRE), or glass (GFRE) fibers.



Plastic (Permanent) Deformation

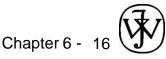
(at lower temperatures, i.e. $T < T_{melt}/3$)



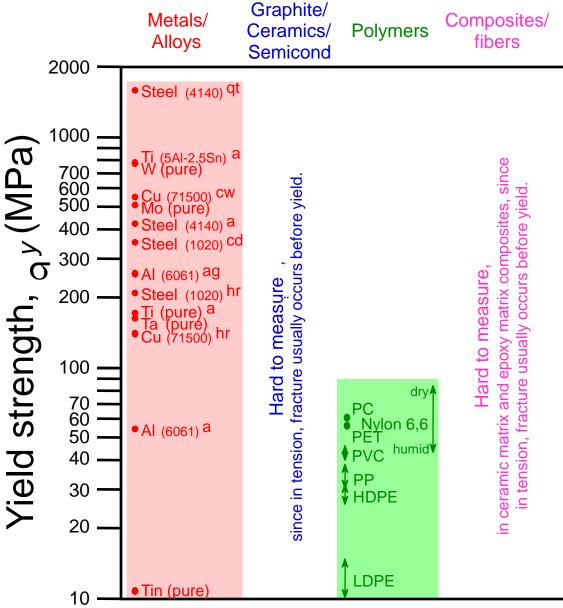


Yield Strength, σ_y

 Stress at which noticeable plastic deformation has occurred. when $\varepsilon_{D} = 0.002$ tensile stress, σ σ_v = yield strength σ_v Note: for 2 inch sample $\varepsilon = 0.002 = \Delta z/z$ $\therefore \Delta z = 0.004$ in engineering strain, ϵ $\epsilon_{p} = 0.002$ Adapted from Fig. 6.10(a), Callister & Rethwisch 8e.



Yield Strength : Comparison



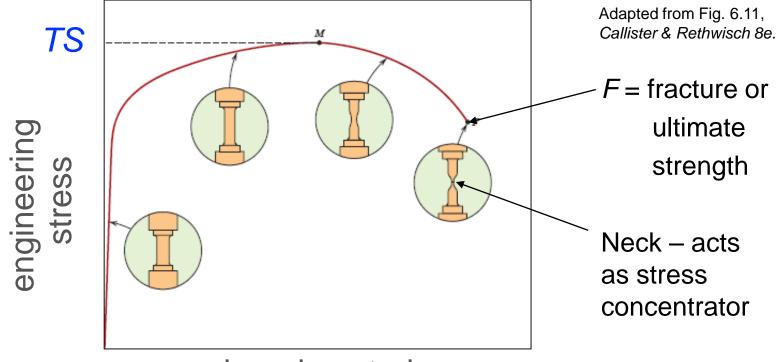
Room temperature values

Based on data in Table B.4, *Callister & Rethwisch 8e.* a = annealed hr = hot rolled ag = aged cd = cold drawn cw = cold worked qt = quenched & tempered



Tensile Strength, TS

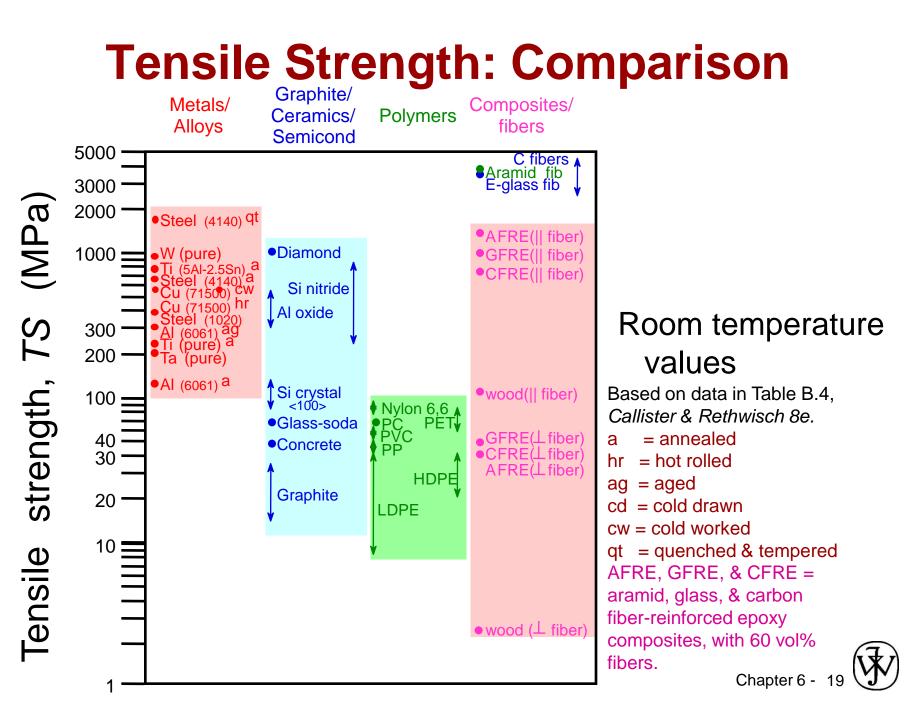
• Maximum stress on engineering stress-strain curve.



engineering strain

- Metals: occurs when noticeable necking starts.
- Polymers: occurs when polymer backbone chains are aligned and about to break.





Ductility

%El Plastic tensile strain at failure: • smaller %EL Engineering

Adapted from Fig. 6.13, Callister & Rethwisch 8e.

tensile

stress, σ

Engineering tensile strain, ε

larger %EL

• Another ductility measure:

$$\% RA = \frac{A_o - A_f}{A_o} \times 100$$

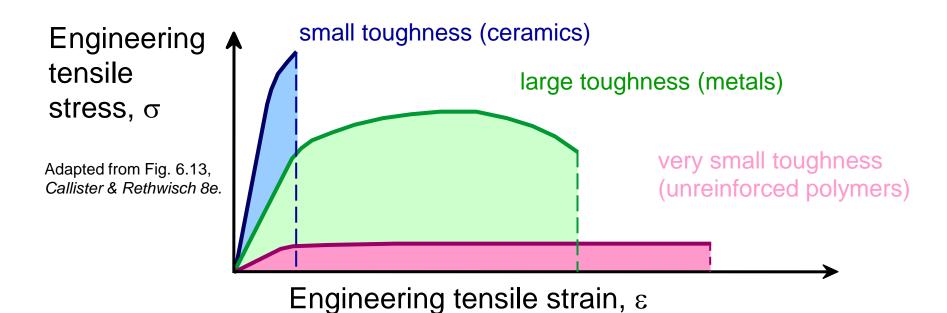
L0



<u>°</u> x 100

Toughness

- Energy to break a unit volume of material
- Approximate by the area under the stress-strain curve.

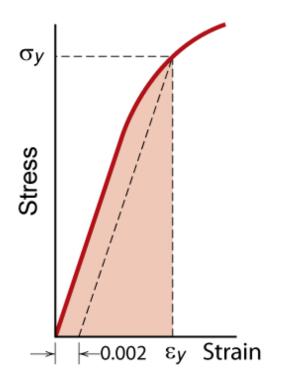


Brittle fracture: elastic energy Ductile fracture: elastic + plastic energy



Resilience, *U_r*

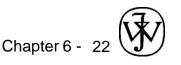
- Ability of a material to store energy
 - Energy stored best in elastic region



$$U_r = \int_0^{\varepsilon_y} \sigma d\varepsilon$$

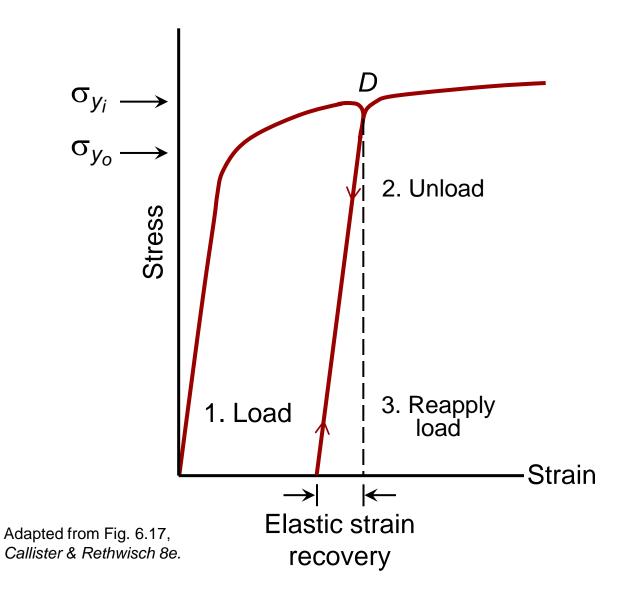
If we assume a linear stress-strain curve this simplifies to

$$U_r \cong \frac{1}{2} \sigma_y \varepsilon_y$$



Adapted from Fig. 6.15, *Callister & Rethwisch 8e.*

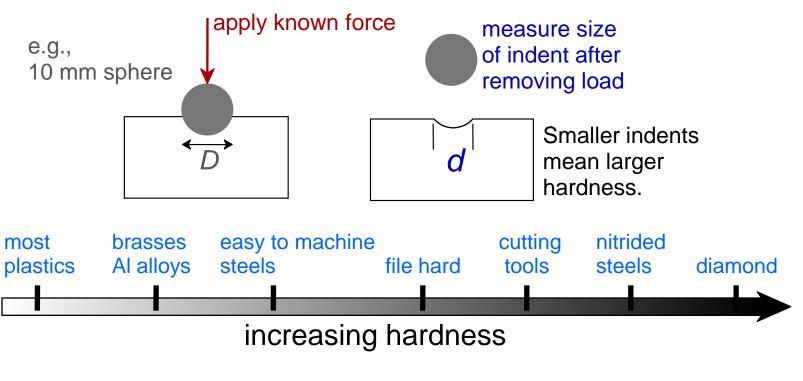
Elastic Strain Recovery





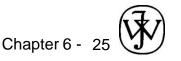
Hardness

- Resistance to permanently indenting the surface.
- Large hardness means:
 - -- resistance to plastic deformation or cracking in compression.
 - -- better wear properties.



Hardness: Measurement

- Rockwell
 - No major sample damage
 - Each scale runs to 130 but only useful in range 20-100.
 - Minor load 10 kg
 - Major load 60 (A), 100 (B) & 150 (C) kg
 - A = diamond, B = 1/16 in. ball, C = diamond
- HB = Brinell Hardness
 - $TS (psia) = 500 \times HB$
 - $TS (MPa) = 3.45 \times HB$



Hardness: Measurement

Table 6.5 Hardness Testing Techniques

Test	Indenter	Shape of Indentation			Formula for
		Side View	Top View	Load	Hardness Number ^a
Brinell	10-mm sphere of steel or tungsten carbide		_;= d ≠	Р	$HB = \frac{2P}{\pi D[D - \sqrt{D^2 - d^2}]}$
Vickers microhardness	Diamond pyramid			Р	$HV = 1.854P/d_1^2$
Knoop microhardness	Diamond pyramid	<i>L/b</i> = 7.11 <i>b/t</i> = 4.00		Р	$\mathbf{HK} = 14.2P/l^2$
Rockwell and Superficial Rockwell	$\begin{cases} Diamond \\ cone \\ \frac{1}{16}, \frac{1}{8}, \frac{1}{4}, \frac{1}{2} \text{ in.} \\ diameter \\ steel spheres \end{cases}$			60 kg 100 kg 150 kg 150 kg 30 kg 45 kg Superficial Rockwell	

^a For the hardness formulas given, P (the applied load) is in kg, while D, d, d₁, and l are all in mm.

Source: Adapted from H. W. Hayden, W. G. Moffatt, and J. Wulff, The Structure and Properties of Materials, Vol. III, Mechanical Behavior. Copyright © 1965 by John Wiley & Sons, New York. Reprinted by permission of John Wiley & Sons, Inc.



True Stress & Strain

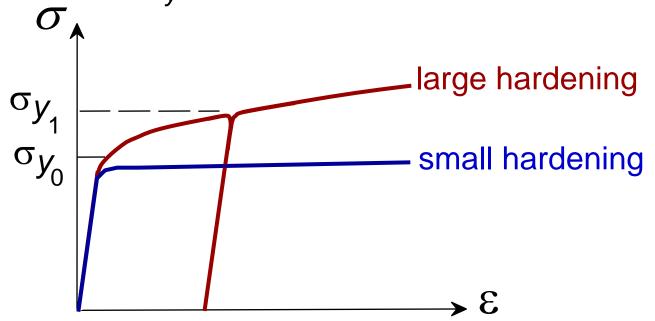
Note: S.A. changes when sample stretched

True stress $\sigma_{\tau} = \sigma \P + \varepsilon$ $\varepsilon_{\tau} = \ln \P + \varepsilon$ $\sigma_T = F/A_i$ $\varepsilon_{\tau} = \ln \langle \ell_i / \ell_o \rangle$ • True strain True M Stress Adapted from Fig. 6.16, М Callister & Rethwisch 8e. Engineering Strain

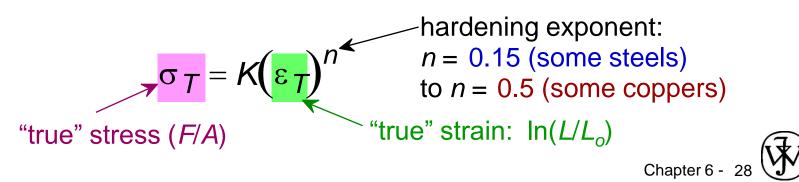


Hardening

• An increase in σ_v due to plastic deformation.

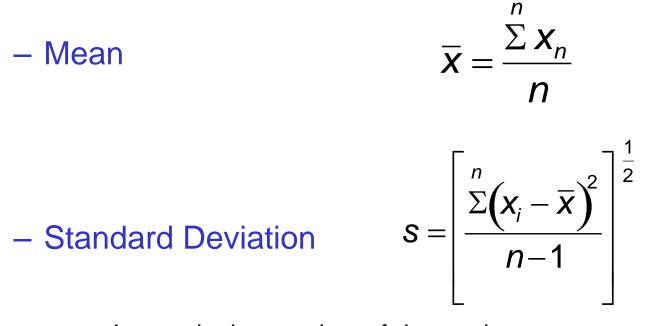


• Curve fit to the stress-strain response:



Variability in Material Properties

- Elastic modulus is material property
- Critical properties depend largely on sample flaws (defects, etc.). Large sample to sample variability.
- Statistics

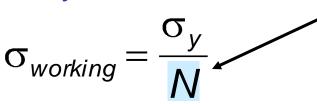


where *n* is the number of data points



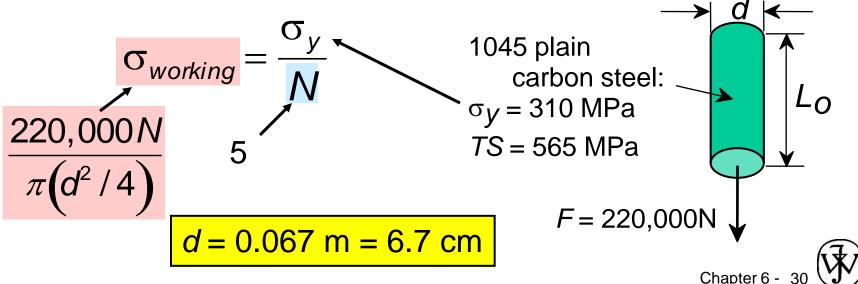
Design or Safety Factors

- Design uncertainties mean we do not push the limit.
- Factor of safety, N



Often *N* is between 1.2 and 4

• Example: Calculate a diameter, *d*, to ensure that yield does not occur in the 1045 carbon steel rod below. Use a factor of safety of 5.



Summary

- Stress and strain: These are size-independent measures of load and displacement, respectively.
- Elastic behavior: This reversible behavior often shows a linear relation between stress and strain. To minimize deformation, select a material with a large elastic modulus (*E* or *G*).
- Plastic behavior: This permanent deformation behavior occurs when the tensile (or compressive) uniaxial stress reaches σ_ν.
- Toughness: The energy needed to break a unit volume of material.
- Ductility: The plastic strain at failure.

