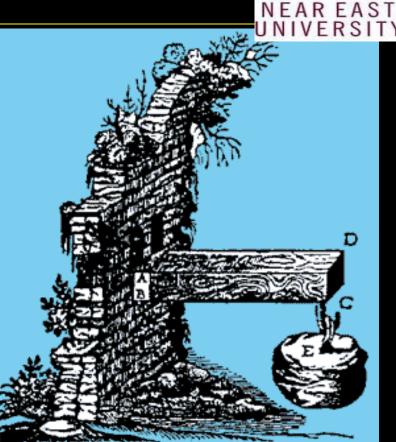
Architectural Structures: Form, Behavior, and Design

Arch 331 hüdaverdi tozan **S**pring 2013

lecture ten

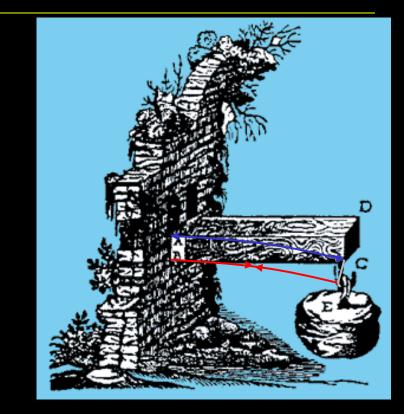
beams: bending and shear stress



Beam Stresses 1 Lecture 10 Architectural Structures ARCH 331 S2013abn

Beam Bending

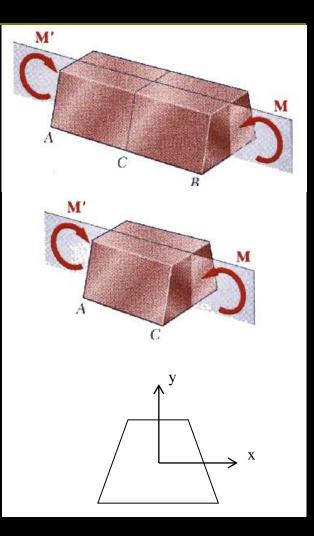
- Galileo
 - relationship between stress and depth²
- can see
 - top squishing
 - bottom stretching



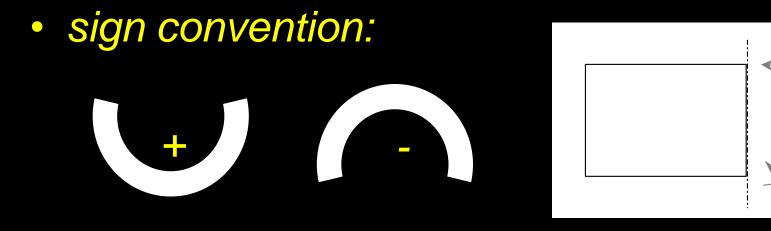
what are the stress across the section?

Pure Bending

- bending only
- no shear
- axial normal stresses from bending can be found in
 - homogeneous materials
 - plane of symmetry
 - follow Hooke's law



Bending Moments



• size of maximum internal moment will govern our design of the section

Normal Stresses

- geometric fit
 - plane sections remain plane
 - stress varies linearly

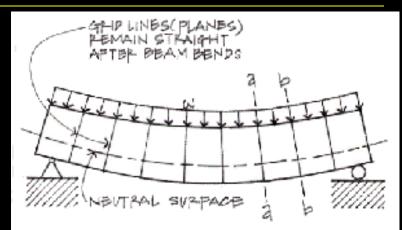
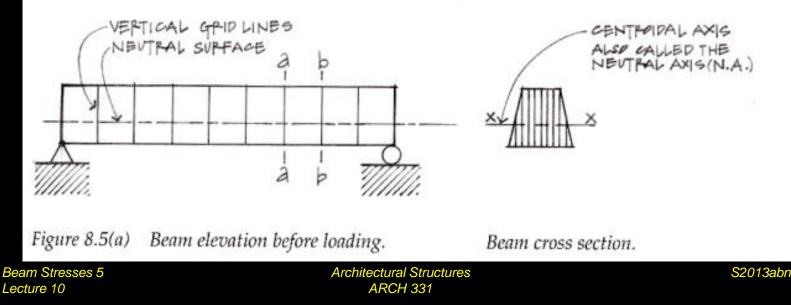


Figure 8.5(b) Beam bending under load.

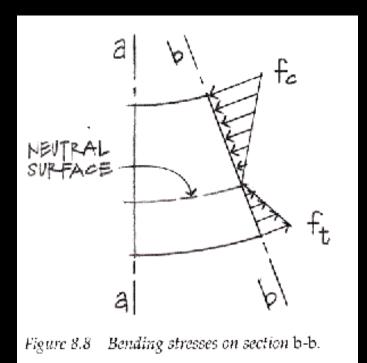


Neutral Axis

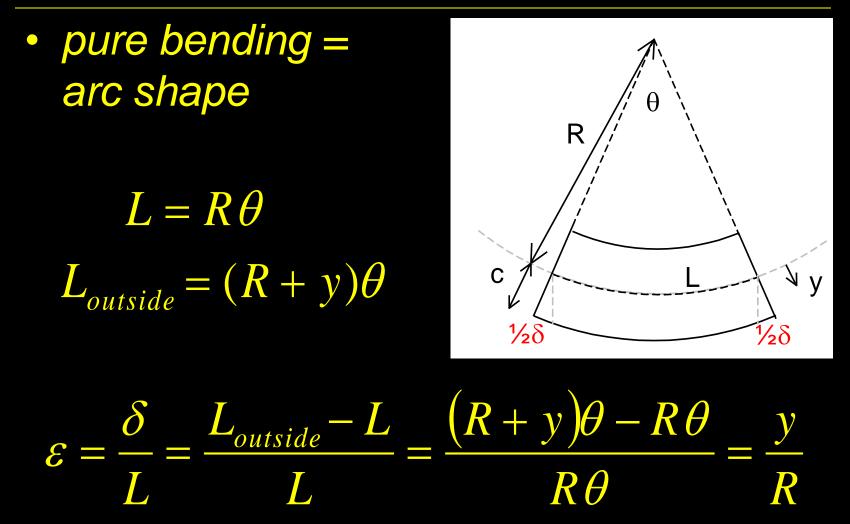
stresses vary linearly

 zero stress occurs at the centroid

 <u>neutral axis</u> is line of centroids (n.a.)



Derivation of Stress from Strain

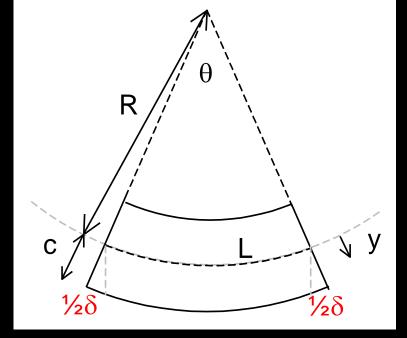


Derivation of Stress

• zero stress at n.a.

$$f = E\varepsilon = \frac{Ey}{R}$$
$$f_{\max} = \frac{Ec}{R}$$

$$f = \frac{y}{c} f_{\text{max}}$$



Beam Stresses 8 Lecture 10



Bending Moment

 resultant moment from stresses = bending moment!

 $M = \Sigma f y \Delta A$

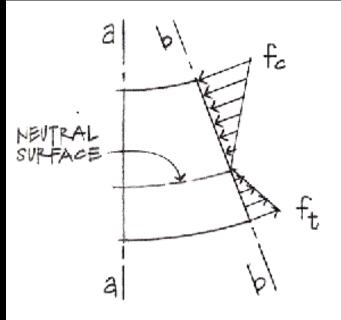
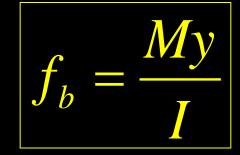


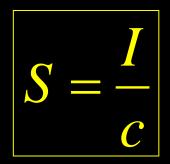
Figure 8.8 Bending stresses on section b-b.

$$= \sum \frac{yf_{max}}{c} y \Delta A = \frac{f_{max}}{c} \sum \frac{y^2 \Delta A}{c} = \frac{f_{max}}{c} I = f_{max}S$$

Bending Stress Relations

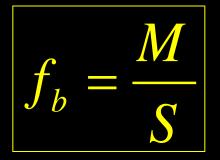






curvature

general bending stress section modulus

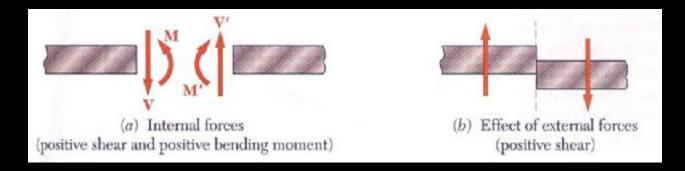


maximum bending stress

required

required section modulus for design

Transverse Loading and Shear



- perpendicular loading
- internal shear
- along with bending moment

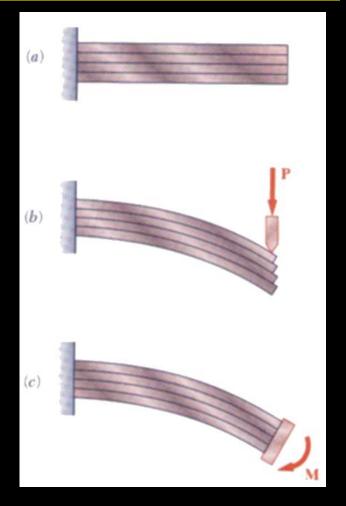


Bending vs. Shear in Design

 bending stresses dominate

 shear stresses exist horizontally with shear

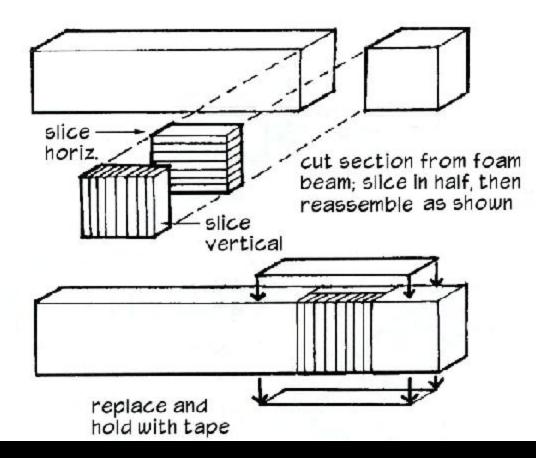
 <u>no shear stresses</u> with pure bending



Beam Stresses 12 Lecture 10 Architectural Structures ARCH 331 S2013abn

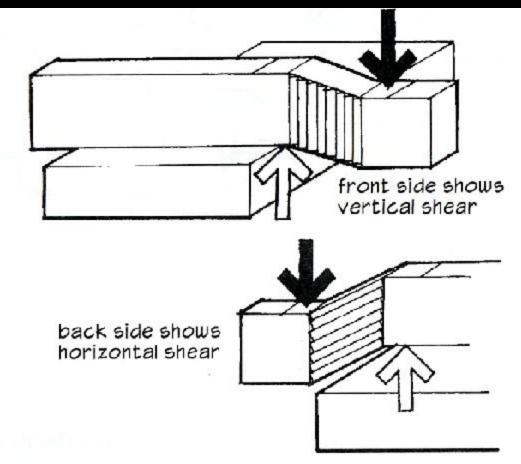
Shear Stresses

horizontal & vertical



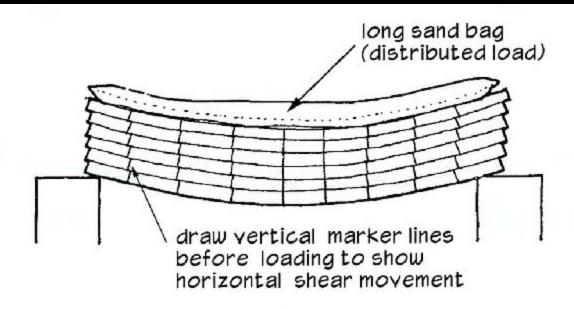
Shear Stresses

horizontal & vertical



Beam Stresses

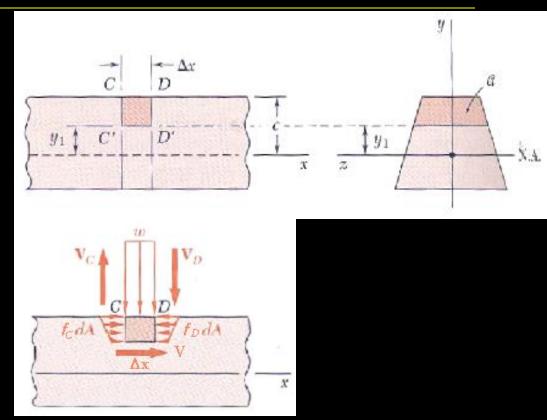
horizontal with bending



Equilibrium

 horizontal force V needed

$$V_{longitudinal} = \frac{V_T Q}{I} \Delta x$$

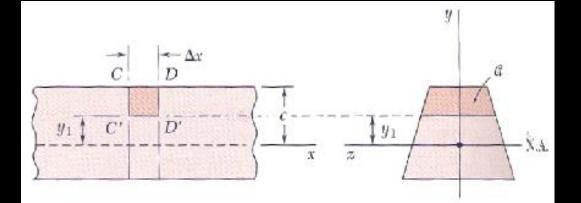


• Q is a moment area

Moment of Area

• Q is a moment area with respect to the n.a. of area <u>above or below</u> the horizontal

 Q_{max} at y=0 (neutral axis)



• *q* is shear flow:

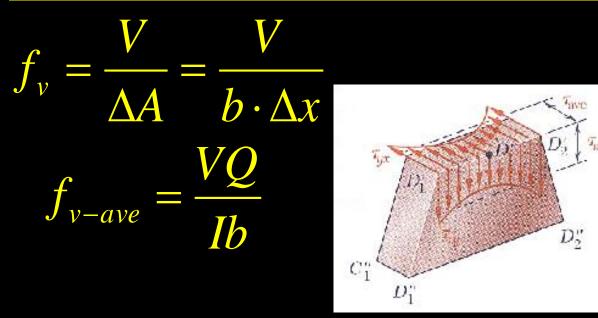
Beam Stresses 17 Lecture 10

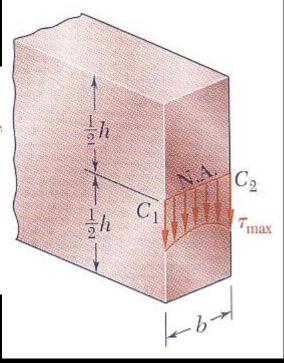
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longitudimal

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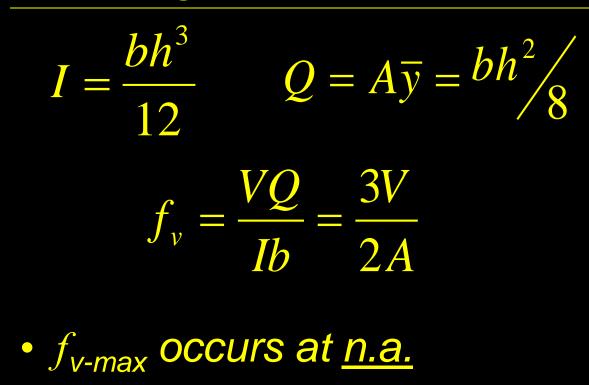
Shearing Stresses

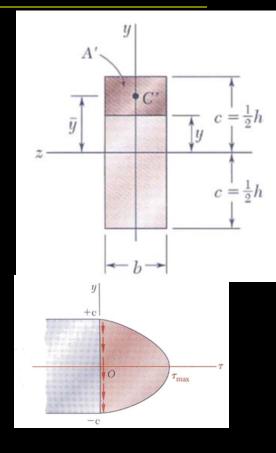




- $f_{v-ave} = 0$ on the top/bottom
- b min may not be with Q max
- with $h/4 \ge b$, $f_{v-max} \le 1.008 f_{v-ave}$

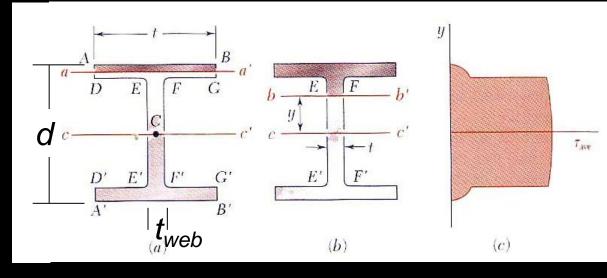
Rectangular Sections



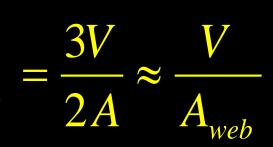


Steel Beam Webs

- W and S sections
 - b varies

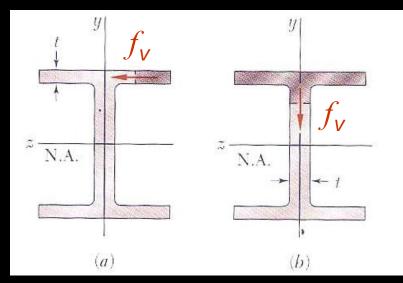


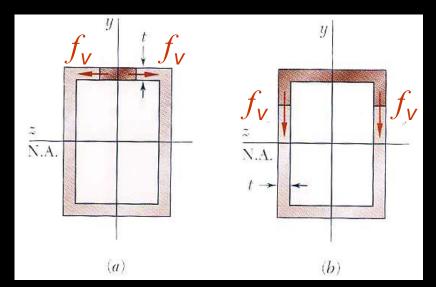
 $\begin{array}{ll} - \mbox{ stress in flange negligible} \\ - \mbox{ presume constant} & f_{v-max} \end{array}$



Shear Flow

- loads applied in plane of symmetry
- cut made perpendicular

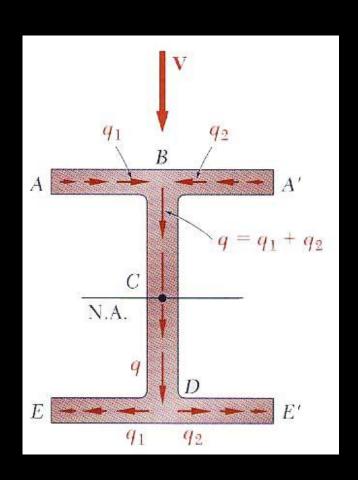




Shear Flow Quantity

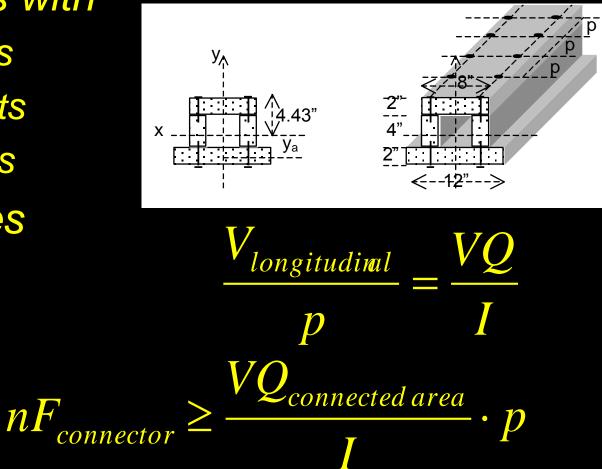
sketch from Q

g



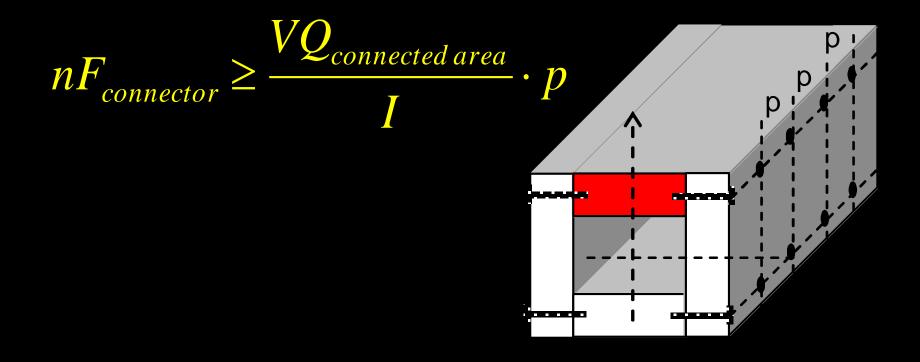
Connectors Resisting Shear

- plates with
 - nails
 - rivets – bolts
- splices



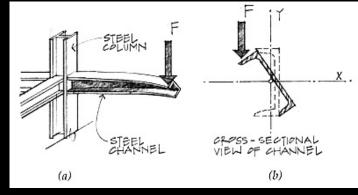
Vertical Connectors

• isolate an area with vertical interfaces



Unsymmetrical Shear or Section

- member can bend and twist
 - not symmetric
 - shear not in that plane
- shear center



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moments balance

